

Algorithm 1, Part 2: Code generation.

Input:

- Sets $Sources(i)$, $1 \leq i \leq q$, represented with affine forms, as produced by Algorithm 1, Part 1; relation R as the result of step 2 of Algorithm 1, Part 1.

Output:

- Code scanning synchronization-free slices and the operations of each slice in lexicographical order for the SCC.

Method:

begin

foreach i , $1 \leq i \leq q$ **do**

 genLoops (in: $Sources(i)$; out: OuterLoops, L_I);

foreach I in L_I **do**

$S_Slice := R * (R_UCS(i) * (I))$

 /* note that if $R_UCS(i) = \emptyset$, then $R_UCS(i) * (I) == I$ */

 genLoops (in: S_Slice ; out: InnerLoops, L_J);

foreach J in L_J **do**

 genLoopBody (in: OuterLoops, InnerLoops, J ; out: LoopBody);

end

where

- $genLoops$ (in: $OperSet$; out: $Loops$, $VectorList$) generates set $Loops$ of loop nests to scan operations comprised in set $OperSet$, and returns a list of corresponding parameterized iteration vectors $VectorList$ comprising the loops index values. To implement function $GenLoops$ any well-known technique, such as [,] can be applied.
- $genLoopBody$ (in: $OuterLoops$, $InnerLoops$, $Iter$; out: $LoopBody$) generates body $LoopBody$ of $InnerLoops$ containing the statements of the source loop to be executed at iteration $Iter$ and inserts loops $InnerLoops$ in the corresponding nest of loops $OuterLoops$. To generate $LoopBody$, the last elements of tuples representing set $InnerLoop$ are taken into consideration (they represent the statement identifiers and allow for choosing appropriate statements to be inserted in the loop body).

An Illustrative Example

To illustrate Algorithm 1, let us consider the following example, which is a slight modification of an example proposed in [].

Example 1.

```
for (i=1; i<=n;i++)  
  
    for (j=1; j<=n;j++) {  
  
s1:        a(i,j)=a(i,j)+ b(i-2,j);  
  
s2:        b(i,j)=a(i,j-2)* b(i,j); }  
  

```

Petit extracts the following dependence relations for this example (see Figure 2).

$R_{12} := \{[i,j] \rightarrow [i,j+2] : 1 \leq i \leq n \ \&\& \ 1 \leq j \leq n-2\}$;

$R_{21} := \{[i,j] \rightarrow [i+2,j] : 1 \leq i \leq n-2 \ \&\& \ 1 \leq j \leq n\}$;

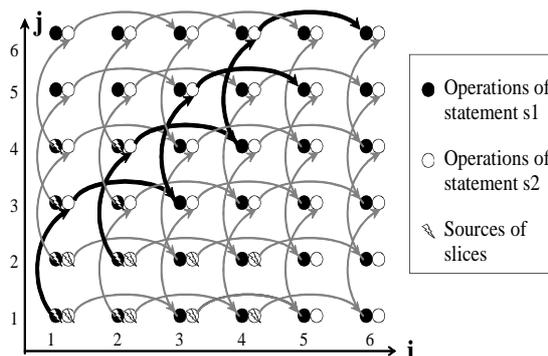


Figure 2. Dependences for Example 1 when $n=6$

To extract slices, to the source loop we can apply the following affine transformations Φ_1 and Φ_2 for statements s_1 and s_2 , respectively: $\Phi_1=i-j$, $\Phi_2=i-j+2$. The transformed loop, for $n=6$, represents 10 independent threads (there is no other affine transformation extracting more than 10 slices). While analyzing Figure 2, we can see that there actually exist 16 independent slices in the source loop. The loop transformed on the basis of the above affine transformations combines some synchronization-free slices together. For example, slices with sources in s_1 (1,1) and s_1 (2,2) (shown in black boldface in Figure 2) are mapped to the same partition. Our approach can be applied to this example as follows, thus extracting all available slices.

Algorithm 1. Part 1.

1. $R_{12}:=\{[i,j,1]\rightarrow[i,j+2,2] : 1\leq i\leq n \ \& \ 1\leq j\leq n-2\};$
 $R_{21}:=\{[i,j,2]\rightarrow[i+2,j,1] : 1\leq i\leq n-2 \ \& \ 1\leq j\leq n\}.$
2. $R:=\{[i,j,2]\rightarrow[i+2,j,1] : 1\leq j\leq n \ \& \ 1\leq i\leq n-2\}\cup\{[i,j,1]\rightarrow[i,j+2,2] : 1\leq j\leq n-2 \ \& \ 1\leq i\leq n\}.$
3. $UDS(1):= \{[i,j,1] : 1\leq j\leq n-2 \ \& \ 1\leq i\leq 2\};$
 $UDS(2):= \{[i,j,2] : 1\leq j\leq 2 \ \& \ 1\leq i\leq n-2\}.$
4. $UDS:= \{[i,j,1] : 1\leq j\leq n-2 \ \& \ 1\leq i\leq 2\} \cup \{[i,j,2] : 1\leq j\leq 2 \ \& \ 1\leq i\leq n-2\}.$
5. For statement 1:
 $R_UCS(1)=\emptyset; Sources(1)=UDS(1)=\{[i,j,1] : 1\leq j\leq n-2 \ \& \ 1\leq i\leq 2\};$
For statement 2:
 $R_UCS(2)=\emptyset; Sources(2)=UDS(2)=\{[i,j,2] : 1\leq j\leq 2 \ \& \ 1\leq i\leq n-2\}.$

Algorithm 1. Part 2.

For statement s_1 :

<p>Generate <u>outer loops</u> to scan the lexicographically minimal sources of synchronization-free slices and being represented with operations of statement s_1 (let us note that for $n<3$ no slices are presented, thus no code is generated).</p>	<pre>if(n>=3) { parfor (t1=1;t1<=2;t1++) for (t2=1;t2<=n-2;t2++) s1(t1,t2,1); }</pre> <p>List L_I contains vector I equal to $(t_1,t_2,1)'$.</p>
<p>Generate <u>inner loops</u> to enumerate operations belonging to the slice with a source represented by vector $I=(t_1,t_2,1)'$ and being contained in set $S_Slice := R^*(R_UCS^*(I)) = \{[i,t_2,1] : i=t_1\} \cup \{[t_1,t_2+2,2] : 1\leq t_1\leq n \ \& \ 1\leq t_2\leq n-2\} \cup \{[i,t_2-t_1+i,1] : \exists (\alpha : 0=t_1+i+2\alpha \ \& \ 1\leq t_1\leq i-2 \ \& \ i\leq n \ \& \ 1\leq t_2 \ \& \ t_2+i\leq t_1+n)\} \cup \{[i,t_2-t_1+i+2,2] : \exists (\alpha : 0=t_1+i+2\alpha \ \& \ 1\leq t_1\leq i-2 \ \& \ i\leq n \ \& \ 2+t_2+i\leq t_1+n \ \& \ 1\leq t_2)\}.$</p>	<pre>s1(t1,t2,1); s1(t1,t2+2,2); for (t3=t1+2;t3<=min(n,t1-t2+n-2);t3+=2) { s1(t3,t2-t1+t3,1); s1(t3,t2-t1+t3+2,2); } for (t3=max(2*intDiv(2*t1-t2+n,2)-t1,t1+2); t3<min(-t2+t1+n,n); t3+=2) s1(t3,t2-t1+t3,1);</pre>
<p>Generate the <u>body of inner loops</u> containing statements of the source loop body to be executed at iteration J, and <u>insert it</u> as the body of outer loops.</p>	<pre>if(n>=3) { parfor (t1=1;t1<=2;t1++) for (t2=1;t2<=n-2;t2++) { a(t1,t2)=a(t1,t2)+b(t1-2,t2); b(t1,t2)=a(t1,t2)*b(t1,t2); for (t3=t1+2;t3<=min(n,t1-t2+n-2);t3+=2) { a(t3,t2-t1+t3)=a(t3,t2-t1+t3)+ b(t3-2,t2-t1+t3); b(t3,t2-t1+t3+2)=a(t3,t2-t1+t3)* b(t3,t2-t1+t3+2); } for (t3=max(2*intDiv(2*t1-t2+n,2)-t1,t1+2); t3<min(-t2+t1+n,n); t3+=2) a(t3,t2-t1+t3)=a(t3,t2-t1+t3)+ b(t3-2,t2-t1+t3); }</pre>

For statement s_2 :

<p>Generate <u>outer loops</u> to scan sources of synchronization-free slices and being operations of statement s_2.</p>	<pre>parfor (t1=1; t1<=n-2; t1++) for (t2=1; t2<=2; t2++) s1(t1,t2,2);</pre> <p>List L_I contains vector I equal to $(t_1,t_2,2)'$.</p>
<p>Generate <u>inner loops</u> to enumerate iterations belonging to the slice with a source represented by vector $I=(t_1,t_2,2)'$ and being contained in set $S_Slice := R^*(R_UCS^*(I)) = \{[i,t_2,2] : i=t_1\} \cup \{[t_1+2, t_2,1] : 1\leq t_1\leq n-2 \ \& \ 1\leq t_2\leq n\} \cup \{[i,t_2-t_1+i,2] : \exists (\alpha : 0=t_1+i+2\alpha \ \& \ 1\leq t_1\leq i-2 \ \& \ i\leq n \ \& \ 2+t_2+i\leq t_1+n \ \& \ 1\leq t_2)\}.$</p>	<pre>s1(t1,t2,2); s1(t1+2,t2,1); if (t2 <= n-2) s1(t1+2,t2+2,2); for (t3=t1+4;t3<= min(t1-t2+n+2,n);t3+= 2) { s1(t3,t2-t1+t3-2,1); s1(t3,t2-t1+t3,2); }</pre>

$\{1 \leq t_1 \leq i-2 \ \& \ i \leq n \ \& \ 1 \leq t_2 \ \& \ t_2+i \leq t_1+n\} \cup \{[i, t_2-t_1+i-1]:$ $\exists (\alpha: 2\alpha=t_1+i \ \& \ 1 \leq t_1 \leq i-4 \ \& \ i \leq n \ \& \ t_2+i \leq 2+t_1+n$ $\ \& \ 1 \leq t_2)\}.$	$\}$
<p>Generate the <u>body of inner loops</u> containing statements of the source loop body to be executed at iteration J, and <u>insert it</u> as the body of outer loops.</p>	<pre> parfor(t1=1; t1<=n-2; t1++) for(t2=1; t2<=2; t2++) { b(t1,t2)=a(t1,t2-2)*b(t1,t2); a(t1+2,t2)=a(t1+2,t2)+b(t1,t2); if (t2<=n-2) s1(t1+2,t2+2,2); for(t3=t1+4;t3<=min(t1-t2+n+2,n);t3+=2){ a(t3,t2-t1+t3-2)=a(t3,t2-t1+t3-2)+ b(t3-2,t2-t1+t3); b(t3,t2-t1+t3)=a(t3,t2-t1+t3-2)* b(t3,t2-t1+t3); } } </pre>

Note that the codes enumerating sources of slices can be executed in parallel, this is denoted with keyword “parfor”